

# ID-Based Directed Multi Proxy Chameleon Signature Scheme with Bilinear Pairing

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**Abstract** — In this paper we first proposed an ID-based directed multi-proxy chameleon signature scheme using bilinear pairings. These schemes allow a group of proxy signers to make a valid proxy chameleon signature for a designated verifier. The designated verifiers only can easily such multi-proxy chameleon signatures generate on behalf of the original signer. Our proposed scheme is secure against existential forgery under adaptive chosen message attack assuming Computational Diffie-Hellman problem as a hard problem.

**Keywords** — Public Key Cryptography, Proxy Chameleon Signature, Bilinear Pairing.

## I. INTRODUCTION

Krawczyk and Rabin [9], introduced chameleon signature. It is in fact a signature based on hash and sign paradigm where chameleon hash function is a trapdoor collision resistant. Chameleon signatures provide non-repudiation and non-transferability for the signed message as the undeniable signatures [4] do, but chameleon signature allows simpler and more efficient realization than the undeniable signature. It is well known fact that chameleon hash function is used to determine the message digest.

The concept of proxy signature was introduced by Mambo et al.[14]. Proxy signature means electronics authentication in which the designated person can sign on behalf of the original signer. Since the invention of proxy signature, several type of proxy signatures have been designed. One among them is noteworthy proxy signature introduced by Hwang and Shi [8]. The advantage of this proxy signature lies with the fact that the original signer can delegate his signing power to many persons not only one. This type of signature scheme is known as multi proxy signature scheme. However, such multi proxy signature scheme fails to provide features like non-repudiation and non-transferability of the signed message. Since chameleon signature had the capacity to deal with such situation, Zhang et al.[19] utilized it to design proxy chameleon signature.

The concept of directed signature scheme was proposed by Lim and Lee [12]. In a directed signature scheme, any signature is generated for a designated verifier, who can directly verify the signature while others know nothing on its validity. In addition, at the time of trouble or if required, both the signer and the designated verifier can verify to a third party that the signature is valid. Later Yang

et al. [18] extended it and made the directed proxy signature scheme. This scheme used the techniques of unforgeable under the Gap Diffie-Hellman Assumption.

Some multi proxy signatures with designated verifier are also given in the literature [11]. In these schemes, an original signer authorized a group of proxy signers and only with the cooperation of all these signers of the proxy group the proxy signatures could be generated for a designated verifier on behalf of the original signer. The designated verifier only can directly verify the multi-proxy signature issue to him. In these schemes, the designated verifier cannot convince any third party about the validity of the multi-proxy signatures scheme otherwise to solve this problem, it necessary to combine the concepts of multi proxy and directedness [10],[13],[16],[17] in order to design a signature.

The concept of ID-based cryptosystem is due to Shamir [15]. Such cryptosystem has the property that the identity information of each user works as his public key. ID-based cryptography has the advantage of easier key distribution as compared to conventional public key cryptography. Ateniese et al.[1],introduced the concept of ID-based chameleon hash function and in the case of chameleon hashing, the advantages of ID-based cryptography are multiplied by the reality that the owner of a public key does not necessarily need to recover the associated secret key. To the best of our knowledge there is no existing scheme with this concept having such intention we thus propose an ID-based directed multi proxy chameleon signature using chameleon hash function involving multi signers. Our proposed scheme is secure against existential forgery under adaptive chosen message attack in the random oracle model assuming Computational Diffie-Hellman problem and maintains the security at par with Zheng et al.[19] in the case of multi signers.

The organization of rest of the paper is as follows: The required preliminaries for proposed design are given in section 2. In section 3, discussion of the design algorithm is given with notations and definitions. The proposed identity-based directed multi proxy chameleon signature is given in section 4. Further an analysis of proposed scheme is described in section 5. In section 6, the security and efficiency aspects of proposed scheme are discussed. Finally, the conclusion of proposed design is given in section 7.

**II. PRELIMINARIES**

First we describe bilinear pairings and Gap Diffie-Hellman group respectively. Next, we present ID-based public key setting for bilinear pairings.

**A. Bilinear Pairing**

Let  $G_1$  be a cyclic additive group generated by  $P$ , whose order is a prime  $q$ , and  $G_2$  be a cyclic multiplicative group of the same order  $q$ . Let  $a$  and  $b$  be the elements of  $Z_q^*$ . We assume that the discrete logarithm problems (DLP) in both the groups  $G_1$  and  $G_2$  are hard. A bilinear pairings is a map  $e : G_1 \times G_1 \rightarrow G_2$  with the following properties:

- Bilinear:  $e(aP, bQ) = e(P, Q)^{ab}$  for all  $P, Q \in G_1$  and  $a, b \in Z_q^*$ .
- Non-degenerate: There exists  $P, Q \in G_1$  such that  $e(P, Q) \neq 1$ .
- Computable: There is an efficient algorithm to compute  $e(P, Q)$  for all  $P, Q \in G_1$ .

**B. Gap Diffie-Hellman Group**

Let  $G_1$  be a cyclic additive group generated by  $P$ , whose order is a prime  $q$ . Assume that the inversion and multiplication in  $G_1$  can be computed efficiently. We first introduce following problems in  $G_1$ :

- Discrete Logarithm Problem (DLP): Given two elements  $P$  and  $Q$ , to find an integer  $n \in Z_q^*$ , such that  $Q = nP$  whenever such an integer exists.
- Computation Diffie-Hellman Problem (CDHP): Given  $P, aP, bP$  for  $a, b \in Z_q^*$ , to compute  $abP$ .
- Decision Diffie-Hellman Problem (DDHP): Given  $P, aP, bP, cP$  for  $a, b, c \in Z_q^*$  to decide whether  $c \equiv ab \pmod q$ .

We call  $G_1$  a Gap Diffie-Hellman Group if DDHP can be solved in polynomial time but there is no polynomial time algorithm to solve CDHP or DLP with non negligible probability. Such group can be found in super singular elliptic curve or hyper elliptic curve over finite field, and bilinear pairings can be derived from the Weil or Tate pairings. For more details, see [2,6, 7].

**III. NOTATIONS AND THE ALGORITHM FOR PROPOSED SCHEME:**

Next we recall notations given in [3,19,20] as below:

Symbol	Description
$G_1$	Cyclic additive group
$G_2$	Cyclic multiplicative group
$q$	Prime Number
$e$	Bilinear Map
$a, b$	Integer number
$P$ and $Q$	Generator of group $G$
$H$	Secure hash function
$r$	Random Number
$SK$	Secret key
$PK$	Public Key
$m$	Message
$\sigma$	Signature
$w$	Warrant
$ID$	Identity
$\parallel$	Concatation

Table 1.

**A. ID-based Direct Multi Proxy Chameleon Signature Scheme**

An ID-based directed multi proxy chameleon signature scheme consists of four entities: original signer, proxy signer group, designer verifier and other party as in charge called Judge who will watch the communication between proxy group and the designer verifier. We define the algorithm for ID-based directed multi proxy chameleon signatures as below:

- a). Setup:-** The private key generator (PKG) runs probabilistic polynomial-time algorithm to generate a pair of keys  $(SK; PK)$  defining the scheme. PKG publishes the system parameters of  $SP$  including the public key  $PK$ , and keeps the master key  $SK$  secret. The input to this algorithm is a security parameter  $1^k$ .
- b). Extract:-** A deterministic polynomial-time algorithm that, on input the master key  $SK$  and an identity string  $ID$ , outputs the trapdoor key associated to the hash key  $S_{ID}$ .
- c). Generation of the Proxy Key:-** This is a protocol between the original signer and all multi proxy signers. The protocol works as follows: The proxy signers take as input their private keys,  $S_A$  on  $ID_A$ , and the delegation warrant  $m_w$  which includes the type of the information delegated. The original signer uses public key and the warrant  $m_w$  with respect to proxy group whose proxy signers sign as the proxy signing key  $SK_{P_i}$  so that original signer and the proxy signer produce proxy chameleon signature on behalf of the original signer.

d). **Chameleon Hash Function:-** A probabilistic polynomial-time algorithm that, on input an identity string  $ID$ , message  $m$ , and a random string  $R$ , outputs the hashed value  $h = Hash(ID, PK, m, R)$ .

e). **Forge:-** A deterministic polynomial - time algorithm  $F$  that, on input  $PK$  the trapdoor key  $S_{ID}$  associated to the identity string  $ID$ , a hash value  $h$  of a message  $m$ , a random string  $R$ , and another message  $m' \neq m$ , outputs a string  $R'$  that satisfies  $h = Hash(ID, PK, m, R) = Hash(ID, PK, m', R')$ .

f). **Dispute:-** Given directed multi proxy chameleon signature  $\sigma_{DMPCS}$  on message  $m$ , the proxy group computes different message  $m'$  and  $R'$ , collision as pair  $(m', R')$ , where  $m' \neq m$  and with the valid signature tuple  $(m', R', \sigma_{DMPCS})$ , the Judge claim that ID-based directed multi proxy chameleon signature of message  $m'$  is forgery.

### B. Security Model

In this section, we give security requirement of the proposed scheme based on [5, 19]: satisfying following properties:

#### Strength:

Distinguishability: Valid directed multi proxy chameleon signatures generated by the proxy signers are distinguishable from valid normal chameleon signatures generated by the original signer.

- **Verifiability:** From the directed multi proxy chameleon signature, a verifier can be convinced of the original signer's contract on the signed message.
- **Unforgeability:** Only the delegated proxy group can generate the proxy signature for a given message on behalf of the original signer. The other party and the original signer not designated as a proxy signer cannot produce a proper chameleon signature which is not generated by the signer earlier.
- **Identifiability:** Any one can identify the proxy signer corresponding to a directed multi proxy chameleon signature.
- **Prevention of misuse:** The proxy signer's cannot use the proxy key for the purpose other than generating a valid directed multi proxy chameleon signature. The other person cannot sign, with the proxy key, the messages which have been not authorized by the authentic signer.
- **Designated Verifiability:** The designated verifier uses their secret key to verify the directed multi proxy chameleon signature generated by a proxy signer's on behalf of the original signer. So the only designated verifier can verify the proxy signature issued to him.

- **Non-Repudiation:** Once a directed multi proxy signer creates a valid directed multi proxy chameleon signature of an original signer, he can't accept the signature creation.
- **Non-Transferability:** Except for the proxy signers himself, no one can prove to another party that the proxy signer's produced a given directed multi proxy chameleon signature.
- **Denial:** The proxy signers can convince the judge to reject a forgery proxy chameleon signature.
- **Message Hiding:** In case of dispute, the proxy signers can compute a new denial the forgery proxy chameleon signature and thus the original message is never revealed.

### IV. THE PROPOSED SCHEME

The proposed scheme involves four characters: The Private Key Generator (PKG), the original signer, group of proxy signers  $PS_i = PS_1, PS_2, \dots, PS_l$  and the recipient. We propose a ID-based directed multi proxy chameleon signature scheme consists of following phases:

1. **Setup:** Let  $G_1$  is a cyclic additive group generated by  $P$  with prime order  $q$ .  $G_2$  is a cyclic multiplicative group of the same order  $q$ .  $e : G_1 \times G_1 \rightarrow G_2$  is a bilinear pairing  $H_0 : \{0,1\}^* \rightarrow G_1, H_1 : \{0,1\}^* \rightarrow Z_q^*$  and  $H_2 : G_2 \times G_1 \rightarrow Z_q^*$  cryptography hash function and  $P_{pub} = sP$ . PKG publishes system parameters  $\{G_1, G_2, e, q, P, P_{pub}, H_0, H_1, H_2\}$ . Here PKG keeps  $s$  as the master-key (Private).

2. **Extract:** Let Alice be the original signer with identity  $ID_A$ , private key be the  $S_A = sQ_{ID_A} = sH_0(ID_A), (PS_i)$  be the proxy signers with identity  $ID_{PS_i}$  and customized identity:  $ID_j = (ID_{recipient} \parallel ID_{Proxysigner} \parallel ID_{transaction})$ , where the identity of the recipient, proxy signer, transaction, and the private key  $(S_{PS_i}) = sQ_{PS_i} = sH_0(ID_{PS_i})$ .

3. **Proxy Key Generation:** To delegate the signing capacity to proxy signers, the original signer uses Hesss ID-based signature scheme [7] to generate the signed warrant  $m_w$  and each proxy signer  $PS_i$  computes his proxy key  $S_{P_i}$ .

-Alice computes  $r_A = e(P, P)^k$ , where  $k \in_R Z_q^*$ , and computes  $c_A = H_2(m_w \parallel ID_A \parallel r_A)$  and  $U_A = c_A S_A + kP$ . Then Alice sends  $(m_w, c_A, U_A)$  to the proxy group L.

- Each  $PS_i$  verifies the validity of the signature on  $m_w$  and computes  $r_A = e(U_A, P)e(Q_A, P_{pub})^{-c_A}$  then accepts this signature if and only if  $c_A = H_2(m_w \| ID_A \| r_A)$ . If the signature is valid,  $PS_i$  computes the proxy key  $S_{P_i}$  as  $S_{P_i} = c_A S_{PS_i} + U_A$ .

**4. Directed Multi Proxy Chameleon Signature Generation:**

**-Hash:** Given a message  $m \in \{0,1\}$ , each  $PS_i$  choose a random element  $R$  from  $G_1$  and calculate the chameleon hash:

$$h = Hash(P_{pub}, m, R, ID_j) = e(R, P)e(H_1(m)H_0(ID_j), P_{pub})$$

**- Forge:** Recipient can make a forgery:

$$R = Forge(P_{pub}, ID_j, S_j, m, R, m') = (H_1(m) - H_1(m')Q_j + R),$$

and accepts this signature if and only if  $c_p = H_2(h \| ID_j \| r_p)$ . The proxy group  $L$  wants to sign a delegated message  $m$  on behalf of the original signer. Each proxy signer  $PS_i$  generates the partial proxy signature to generate directed multi proxy signature.

-Each:  $PS_i$  randomly selects an integer  $k_i, k_j \in_R Z_q^*$ , compute  $r_{P_i} = e(P, P)^{k_i}$ ,  $L_{P_i} = e(S_{PS_i}, Q_v)^{k_j}$  and broadcasts  $r_{P_i}, L_{P_i}$  to the remaining  $l - 1$  proxy signers. Then compute

$$r_p = \prod_{i=1}^l r_{P_i} \text{ and } L_p = \prod_{i=1}^l L_{P_i}$$

and  $U_{P_i} = c_p S_{P_i} + k_{P_i} P$ . Finally, the individual proxy signature of the message  $m$  is  $(c_p, U_{P_i})$ .

and  $c_p = H_2(h \| ID_j \| r_p)$ . Once all individual proxy chameleon signatures are correct, then thus computes

$$U_p = \prod_{i=1}^l U_{P_i}$$

The valid directed multi-proxy chameleon signature is therefore the tuple:  $\langle m, R, c_p, U_p, m_w, r_A \rangle$ .

**5. Verification:** Verification phase is divided into two parts as described on our scheme. First is direct verification and other is the public verification.

**(A) Direct verification:** Given identity  $ID$ , the designated verifier  $v$  first calculate

$$r_p = e(U_p, P)(e(\sum_{i=1}^l (Q_A + Q_{PS_i}), P_{pub})^{c_A}, r_A^l)^{-c_A}$$

and accepts the signature if and only if

$$c_p = H_2(h \| ID_j \| r_p).$$

**(B)Public Verification:** Given a signature  $\langle m, R, c_p, U_p, m_w, r_A \rangle$  on signer  $ID_s$ , verifier

$ID_v$  and message  $m$ , to enable third party  $J$  to verify it either signer and verifier  $ID$  compute  $Aid = L_p$  provide by either the employees or designated verifier  $ID$ . Now with this  $Aid$ ,  $J$  compute

$$r_p = e(U_p, P)(e(\sum_{i=1}^l (Q_A + Q_{PS_i}), P_{pub})^{c_A}, r_A^l)^{-c_p}.$$

$J$  accepts the signature if and only if  $c_p = H_2(h \| ID_j \| r_p)$ .

**Dispute:** In the case of dispute up on the validity of the signature the following case arises: to generate collision in the chameleon hash function, for a given forgery  $(m', R', c_p, U_p, m_w, r_A)$ , the recipient employee uses to compute the multi proxy chameleon signature up on original message  $m$ .

**Input:** The process is

$$Hash(P_{pub}, m, R, ID_j) = Hash(P_{pub}, m', R', ID_j)$$

where  $m' \neq m$  and proxy signers calculate

$$t = \frac{R' - R}{H_1(m) - H_1(m')}.$$

- Proxy signers choose any message  $\tilde{m}$  and computes  $\tilde{R} = (H_1(m) - H_1(m')Q_j + R)$

**Output:** Output is  $(\tilde{m}, \tilde{R})$  with the tuple  $(\tilde{m}, \tilde{R}, c_p, U_p, m_w, r_A)$ , proxy signer can convince the judge  $J$  to reject the false proxy chameleon signature  $(m', R', c_p, U_p, m_w, r_A)$ .

-Judge  $J$  applies the above verification algorithm. If this verification fails then the alleged signature is rejected by  $J$ , Otherwise;

-  $J$  summons the proxy signer to deny/accept the signature.

**V. CORRECTNESS OF THE PROPOSED SCHEME**

The correctness of the signature is justified by the following equations: chameleon signature and ID-based directed multi proxy chameleon signature have the same algorithm for chameleon hashing. Therefore the following proofs of correctness owes much to the [7,20]. The forgery equation is.

$$\begin{aligned} & Hash(P_{pub}, m', R', ID_j) \\ &= e(R', P)e(H_1(m')H_0(ID_j), P_{pub}) \\ &= e((H_1(m) - H_1(m')Q_j + R), P)e(H_1(m')Q_j, P_{pub}) \\ &= e(H_1(m) - H_1(m')Q_j, P)e(R, P)e(H_1(m')Q_j, P_{pub}) \\ &= e(R, P)e(H_1(m) - H_1(m')Q_j, P)e(H_1(m')Q_j, P_{pub}) \\ &= e(R, P)e(H_1(m) - H_1(m')H_0(ID_j), P_{pub})e(H_1(m')H_0(ID_j), P_{pub}) \\ &= e(R, P)e(H_1(m)H_0(ID_j), P_{pub}) \\ &= Hash(P_{pub}, m, R, ID_j) \end{aligned}$$

**Verifiability:** The verification and correctness of the ID-based directed multi proxy chameleon signature is justified by the equation:

$$\begin{aligned}
 & e(U_p, P) \left( e \left( \sum_{i=1}^l (Q_A + Q_{PS_i}), P_{pub} \right)^{c_A} \cdot r_A^l \right)^{-c_P} \\
 &= e \left( \sum_{i=1}^l U_{p_i}, P \right) e \left( \sum_{i=1}^l (S_A + S_{PS_i}), P \right)^{c_A} \cdot r_A^l)^{-c_P} \\
 &= e \left( \sum_{i=1}^l U_{p_i}, P \right) e \left( \sum_{i=1}^l (S_{p_i} - kP), P \right) \cdot r_A^l)^{-c_P} \\
 &= e \left( \sum_{i=1}^l c_p S_{p_i} + k_{p_i} P, P \right) e \left( \sum_{i=1}^l (S_{p_i}, P) \right)^{-c_P} \\
 &= e \left( \sum_{i=1}^l k_{p_i} P, P \right) \\
 &= \prod_{i=1}^l r_{p_i} \\
 &= r_p
 \end{aligned}$$

**VI. SECURITY ANALYSIS OF PROPOSED SCHEME**

**Theorem 1.** The proposed ID-based directed multi proxy chameleon signature scheme enjoys all advantages of proxy signature schemes [19] i.e Distinguishing ability, Verifiability, Identifiability, Prevention of misuse, Non-forgery ability, Designated verifiability, non-repudiation, Non-transferability, Denial and Message hiding.

**Proof. Distinguishability:** It is evident that the valid ID-based directed multi-proxy chameleon signatures are distinguishable from normal valid multi proxy chameleon signatures generated by anyone.

**Verifiability:** The verifier can be made convinced that the proxy signers have the original signers signature on the warrant  $m_w$  and warrant contain identity information and delegated signing capacity to verify, with the verification tuple  $(m, R, c_p, U_p, m_w, r_A)$  from the construction of  $(c_p, U_p, r_A)$  in directed multi proxy chameleon signature verification scheme.

**Non-forgery:** The proxy group can generate the ID-based directed multi proxy chameleon signature for a given message  $m'$  and the original signer is signature on warrant  $m_w$ . Even if some adversary wants to forge the multi-proxy signature of the message  $m'$  for the proxy group and the original signer Alice. But he cannot forge this signature, since our scheme is based on Hess's [7], ID-based signature scheme, which is proved to be secure against existential forgery on adaptive chosen message attacks under the random oracle model assuming CDH Problem is hard. On the other hand, the original signer cannot create a valid directed multi-proxy signature since each proxy key includes the private key  $SP_i$  of each proxy signer. Assume

that the adversary wants the proxy group to sign the false message  $m'$ . He can change his  $r_{p_i}$ , therefore  $rP$  can be changed, but from the security of the basic ID-based signature scheme and public one way hash function H1, it is impossible for the adversary to get  $c'_p$  and  $U'_p$  such that  $\langle m', c'_p, U'_p, m_w, r_A \rangle$  is a valid ID-based directed multi-proxy chameleon signature.

**Identifiability:** The identities of public key of all proxy signers are involved in the verification of the ID-based directed multi proxy chameleon signature. Therefore any one can identify all the proxy chameleon signatures.

**Prevention of Misuse:** An ID-based directed multi proxy chameleon signature scheme due to use of the warrant  $m_w$ , the proxy group can sign message only that have been authorized by the original signer, nothing else.

**Designated Verifiability:** The designated verifier  $v$  on  $ID$  has to use his secret key  $sQ_A$  at the time of verification of the directed multi-proxy signature. So, the only designated verifier can directly verify the validity of the proxy signature. No one can verify the validity of the ID-based directed multi-proxy signature without the help of either the designated verifier  $v$  on  $ID$  or the designated employees.

**Non-repudiation:** The proxy signers generated by valid ID-based directed multi proxy chameleon signature can generate  $(m, R, c_p, U_p, m_w, r_A)$ , but those proxy signers cannot generate other signature  $(m', R', c_p, U_p, m_w, r_A)$ , where  $m' \neq m$ . This is equivalent to finding a collision of the Id-based chameleon hash function, assuming CDHP hard.

**Non-Transferability:** Proxy signers generate ID-based directed multi proxy chameleon signature for recipient and compute a random value on message  $m$  then the equation  $R' = (H_1(m) - H_1(m')Q_j + R)$  and  $Hash(P_{pub}, m, R, ID_j) = Hash(P_{pub}, m', R'ID_j)$  has the hash value. Hence our ID-based directed multi proxy chameleon signature verify the correct value is  $(m', R', c_p, U_p, m_w, r_A)$ . Thus we see that the recipient can not the convince a third party because  $m'$  have exactly one value  $R'$ .  $R'$  produces proper signature tuple which is nothing efficient computation.

**Denial:** In the proposed scheme the proxy signers can convince the judge to reject a forgery directed multi proxy chameleon signature i.e proxy signers and the recipient can give the authority to judge  $J$  from recipient signature  $(\tilde{m}, \tilde{R}, c_p, U_p, m_w, r_A)$ . If any proxy signer wants to claim that the signature is invalid, he needs to provide a collision in the hash function, the value  $m' \neq m$  and a value  $R'$  such that  $Hash(P_{pub}, ID_j, \tilde{m}, \tilde{R}) = Hash(P_{pub}, ID_j, m, R)$

In this case the ID-based directed multi proxy chameleon signature  $\sigma_{DMPCS}$  is originally generated by proxy signers with the pair  $(m, R) \neq (\tilde{m}, \tilde{R})$ .

**Message Hiding:** During, the message hiding process in ID-based directed multi proxy chameleon signature, the original signer constructs another false signature for any message with the same element of directed multi proxy chameleon signature. Original signer do not disclose the original message.

**Key Exposure Freeness**

As per the algorithm given in [1,9] If a recipient with identity  $ID_c$  has never computed a collision under a customized identity  $ID_j$ , then there is no efficient method for an adversary to find a collision for a given chameleon hash value in DMPCS other then  $Hash(P_{pub}, ID_j, m, R)$ .

This must remain true even if the adversary has oracle access to  $F$  and is permitted polynomial many queries on triples  $(ID_j, m_j, R_j)$  of his choice, except that  $ID_j$  is not allowed to equal the challenge  $ID$ .

**A. Efficiency**

The proposed scheme has computational cost abbreviated as follows:

Notation	Definition
$MulG_2$	Multiplication in the group
$Mul$	Multiplication
$H_1$ and $H_2$	Hash function
$Exp$	Exponent
$M_2P$	Map -to-Point
$Add$	Addition
$Pa$	Pairing
$Sum$	Summation

Table 2.

Phase	Set - up	Extract	Key Gen	Sig- Gen	Directed verify	Pub. verify
$H_1$			2	1		
$H_2$				1		
$Exp$			2		3	3
$M_2P$		2		1		
$Mul$	1		3	3		
$Add$			2	1	1	1
$MulG_2$			1	1	1	1
$Pa$			2	3	1	1
$Sum$			1		1	1

Table 3.

As per above table, to view the efficiency of proposed scheme during different phases the cost is estimated as below:

- The setup phase is  $1Mul$
- Extract phase is  $2M_2P$
- Key generation is  $2H_1 + 2Exp + 3Mul + 12Add + 1Mul + 2Pa + 1Sum$
- Signature generation is  $1H_1 + 1H_2 + 1M_2P + 3Mul + 1Add + 1MulG_2 + 2Pa$
- Verification is  $3Exp + 1Add + 1MulG_2 + 2Pa + 1Sum$

**VII. CONCLUSIONS**

We first proposed an ID-based direct multi proxy chameleon signature scheme with bilinear pairing scheme. Our scheme is based on Hess's [7] scheme, which is more secure against existential forgery under adaptive chosen message attack in the random oracle model. So we can see that our scheme is secure from existential forgery attack, using Computational Diffie-Hellman problem.

**ACKNOWLEDGMENT**

The author is thankful to UGC, New Delhi, India for providing Rajiv Gandhi National fellowship (F1-17.1/2010-13/RGNF-2012-13-ST-CHH-35416) as financial assistance for this Research work.

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